## Practical Geometry

## To construct a quadrilateral when four sides and one diagonal are given

Example. Construct a quadrilateral ABCD given that $\mathrm{AB}=5.5 \mathrm{~cm}, \mathrm{BC}=4 \mathrm{~cm}, \mathrm{CD}=4.5 \mathrm{~cm}, \mathrm{DA}=3$ cm and the diagonal $\mathrm{AC}=4 \mathrm{~cm}$.

## Steps of construction:

1. Draw $\mathrm{AC}=4 \mathrm{~cm}$.
2. With A as centre and a radius 3 cm draw an arc on one side of AC .
3. With C as centre and radius 4.5 cm draw an arc cutting the first arc at D .
4. Join A to D and also C to D .
5. With A as centre and radius 5.5 cm draw an arc on the other side of AC .
6. With C as centre and radius 4 cm draw another arc cutting the previous arc at B .
7. Join A to B and also C to B . Then ABCD is the required quadrilateral.


B
Notes : 1. Since four sides and a diagonal of quadrilateral are given, it is convenient to think that it is made up of two triangles on opposite sides of a common base.
2. Sum of any two sides of a triangle is greater than the third side.

To construct a quadrilateral when four sides and one angle are given :
Example. Construct a quadrilateral ABCD , having given $\mathrm{AB}=3.5 \mathrm{~cm}, \mathrm{BC}=4 \mathrm{~cm}, \mathrm{CD}=4.5 \mathrm{~cm}$, $\mathrm{DA}=5 \mathrm{~cm}$ and $\angle \mathrm{B}=60^{\circ}$

## Steps of Construction

1. $\operatorname{Draw~} \mathrm{AB}=3.5 \mathrm{~cm}$.
2. At $B$ draw $\angle \mathrm{ABY}=60^{\circ}$.
3. Cut off from $B Y$, a segment $B C=4 \mathrm{~cm}$.
4. With A as centre and radius 5 cm draw an arc.
5. With C as centre and radius 4.5 cm draw an arc cutting the first arc at D .
6. Join A to D and also C to D . Then ABCD is the required quadrilateral.


To construct a quadrilateral when three sides and two diagonals are given :
Example. Construct a quadrilateral ABCD , given that $\mathrm{AB}=4 \mathrm{~cm}, \mathrm{BC}=3 \mathrm{~cm}, \mathrm{AD}=3.5 \mathrm{~cm}$, diagonal $\mathrm{AC}=5 \mathrm{~cm}$ and diagonal $\mathrm{BD}=6 \mathrm{~cm}$.

## Steps of Construction:

1. Draw $\mathrm{BC}=3 \mathrm{~cm}$.
2. With $B$ as centre and radius 4 cm draw an arc.
3. With C as centre and radius 5 cm draw an arc cutting the first arc at A .
4. Join B to A and also C to A.
5. With A as centre and radius 3.5 cm draw an arc.
6. With B as centre and radius 6 cm draw an arc cutting the first arc at D .
7. Join C to $\mathrm{D}, \mathrm{B}$ to D and also A to D .

Then ABCD is the required quadrilateral.



## To construct a quadrilateral when three sides and two included angles are given :

Example. Construct a quadrilateral ABCD , given that $\mathrm{AB}=5 \mathrm{~cm}, \mathrm{BC}=4.5 \mathrm{~cm}, \mathrm{CD}=4 \mathrm{~cm}, \angle \mathrm{~B}=60^{\circ}$ and $\angle \mathrm{C}=135^{\circ}$.

## Steps of Construction:

1. Draw $\mathrm{BC}=4.5 \mathrm{~cm}$.
2. At B and C draw angles of $60^{\circ}$ and $135^{\circ}$ respectively.
3. Cut off $\mathrm{BA}=5 \mathrm{~cm}$ and $\mathrm{CD}=4 \mathrm{~cm}$.
4. Join A to D.

Then ABCD is the required quadrilateral.


To construct a quadrilateral when two adjacent sides and three angles are given :

Example. Construct a quadrilateral ABCD , given that $\mathrm{AB}=5 \mathrm{~cm}, \mathrm{BC}=4 \mathrm{~cm}, \angle \mathrm{~B}=60^{\circ}, \angle \mathrm{A}=90^{\circ}$ and $\angle \mathrm{C}=135^{\circ}$.

## Steps of construction:

1. Draw $\mathrm{AB}=5 \mathrm{~cm}$.
2. At B draw $\angle \mathrm{ABY}=60^{\circ}$.
3. From BY cut off $B C=4 \mathrm{~cm}$.
4. At A draw $\angle \mathrm{BAX}=90^{\circ}$.
5. At C draw $\angle \mathrm{BCD}=135^{\circ}$, so that its arm CD cuts AX at D .

Then ABCD is the required quadrilateral.


> Note: We know that sum of the angles of a quadrilateral is $360^{\circ}$. Hence the sum of the given three angles should be less than $360^{\circ}$.

## Construction of special types of quadrilaterals :

We have learnt earlier some properties of the parallelograms, we are now in a position to construct parallelograms, rectangles, squares, rhombuses and trapeziums when a suitable number of elements are given.

Example 1. Construct a parallelogram ABCD , given that $\mathrm{AB}=3.5 \mathrm{~cm}, \mathrm{BC}=5.5 \mathrm{~cm}$ and $\angle \mathrm{B}=75^{\circ}$.

## Steps of Construction:

1. Draw $\mathrm{BC}=5.5 \mathrm{~cm}$.
2. At B draw $\angle \mathrm{CBY}=75^{\circ}$.
3. From BY, cut off $\mathrm{BA}=3.5 \mathrm{~cm}$.
4. With A as centre and radius 5.5 cm draw an arc.
5. With C as centre and radius 3.5 cm draw another arc cutting the first arc at D .
6. Join A to D and C to D.

Then ABCD is the required parallelogram.


Example 2. Construct a parallelogram ABCD , given that $\mathrm{AC}=4.5 \mathrm{~cm}$ and $\mathrm{BD}=4 \mathrm{~cm}$ and the angle between the diagonals is $30^{\circ}$.

## Steps of Construction:

1. Draw $\mathrm{AC}=4.5 \mathrm{~cm}$.
2. Draw PQ , the perpendicular bisector of AC meeting AC at O .
3. Through O draw a line XY , making $\angle \mathrm{XOC}=30^{\circ}$.
4. Cut of $\mathrm{OD}=\mathrm{OB}=2 \mathrm{~cm}\left(=\frac{1}{2} \mathrm{BD}\right)$ from XY .
5. Join A to B, B to C, C to D and A to D.

Then ABCD is the required parallelogram.


Example 3. Construct a square ABCD , given that diagnonal $\mathrm{AC}=6 \mathrm{~cm}$.

## Steps of Construction:

1. Draw a segment $\mathrm{AC}=6 \mathrm{~cm}$.
2. Draw XY , the right bisector of AC meeting AC at O .
3. Cut off $\mathrm{OD}=\mathrm{OB}=3 \mathrm{~cm}\left(=\frac{1}{2} \mathrm{AC}\right)$ from OX and OY respectively.
4. Join A to $\mathrm{B}, \mathrm{B}$ to $\mathrm{C}, \mathrm{C}$ to D and A to D . Then ABCD is the required square.


Note : Diagonals of a square are equal and bisect each other at right angles.
Example 4. Construct a rectangle ABCD whose diagonal $\mathrm{AC}=6 \mathrm{~cm}$ and the angle between the diagonals is $30^{\circ}$.

## Steps of Construction:

1. Draw $\mathrm{AC}=6 \mathrm{~cm}$.
2. Bisect AC at O .
3. At O , draw XY making $\angle \mathrm{COX}=30^{\circ}$.
4. Cut off $\mathrm{OB}=\mathrm{OD}=3 \mathrm{~cm}\left(=\frac{1}{2} \times \mathrm{AC}\right)$.
5. Join A to B, B to C, C to D and A to D. Then ABCD is the required rectangle.


Example 5. Construct a rhombus ABCD whose diagonals AC and BD are 7 cm and 5 cm respectively.

## Steps of Construction:

1. Draw $\mathrm{AC}=7 \mathrm{~cm}$.
2. Draw PQ the perpendicular bisector of AC , meeting AC at O .
3. From OP and OQ cut off $\mathrm{OD}=\mathrm{OB}=2.5 \mathrm{~cm}\left(=\frac{1}{2} \mathrm{BD}\right)$ respectively.
4. Join A to B, B to C, C to d and D to A.

Then ABCD is the required rhombus.

## Note: Diagonals of a rhombus bisect each other at right angles.



## IMPORTANT TIPS FOR COMPETITIVE EXAMS

1. The figure formed by four line segments is called a quadrilateral.
2. A quadrilateral has four sides, four angles and two diagonals.

3 A quadrilateral in which the measure of each angle is less than $180^{\circ}$ is known as a convex quadrilateral
4. A quadrilateral in which one of the angles measures more than $180^{\circ}$ is known as a concave quadrilateral
5. The sum of all angles in a quadrilateral is $360^{\circ}$.
6. To construct a quadrilateral, we need five measurements.

## REVISION EXERCISE

## LEVEL - I

1. Construct a quadrilateral ABCD given that $\mathrm{AB}=3 \mathrm{~cm}, \mathrm{BC}=3.5 \mathrm{~cm}, \mathrm{CD}=4 \mathrm{~cm}, \mathrm{DA}=5.5 \mathrm{~cm}$ and $\mathrm{AC}=6 \mathrm{~cm}$.
2. Is it possible to construct a quadrilateral in which $\mathrm{AB}=3 \mathrm{~cm}, \mathrm{BC}=4 \mathrm{~cm}, \mathrm{CD}=5.4 \mathrm{~cm}, \mathrm{DA}=4.9 \mathrm{~cm}$ and diagonal $\mathrm{AC}=8 \mathrm{~cm}$ ? If not why?
3. Construct a quadrilateral ABCD in which $\mathrm{AB}=4 \mathrm{~cm}, \mathrm{BC}=4.5 \mathrm{~cm}, \mathrm{CD}=5 \mathrm{~cm}, \mathrm{DA}=4.5 \mathrm{~cm}$ and $\angle \mathrm{C}=60^{\circ}$.
4. Construct a quadrilateral ABCD , having given $\mathrm{AB}=4 \mathrm{~cm}, \mathrm{BC}=4.5 \mathrm{~cm}, \mathrm{AD}=4 \mathrm{~cm}, \mathrm{AC}=6 \mathrm{~cm}$ and $\mathrm{BD}=6.5 \mathrm{~cm}$.
5. Construct a quadrilateral PQRS in which $\mathrm{PQ}=5 \mathrm{~cm}, \mathrm{RS}=4 \mathrm{~cm}, \mathrm{PS}=8 \mathrm{~cm}, \mathrm{PR}=10 \mathrm{~cm}$ and $\mathrm{QS}=7 \mathrm{~cm}$. Measure the fourth side.
6. Construct a quadrilateral PQRS in which $\mathrm{PQ}=3 \mathrm{~cm}, \angle \mathrm{Q}=80^{\circ}, \mathrm{PR}=6 \mathrm{~cm}$ and $\mathrm{PS}=\mathrm{RS}=5 \mathrm{~cm}$
7. Construct q quadrilateral ABCD , given that $\mathrm{AB}=4 \mathrm{~cm}, \mathrm{BC}=4.5 \mathrm{~cm}, \mathrm{CD}=5 \mathrm{~cm}, \angle \mathrm{~B}=75^{\circ}$ and $\angle \mathrm{C}=100^{\circ}$.
8. Construct a quadrilateral PQRS in which $\mathrm{RS}=6 \mathrm{~cm}, \mathrm{QR}=5 \mathrm{~cm}, \mathrm{PQ}=5 \mathrm{~cm} \angle \mathrm{Q}=135^{\circ}, \angle \mathrm{R}=90^{\circ}$. Measure PS.
9. Construct a quadrilateral ABCD in which $\mathrm{BC}=4.5 \mathrm{~cm}, \mathrm{AB}=4 \mathrm{~cm}, \angle \mathrm{~B}=75^{\circ}, \angle \mathrm{A}=90^{\circ}$ and $\angle \mathrm{C}=120^{\circ}$.
10. Is it possible to construct a quadrilateral PQRS in which $\mathrm{PQ}=4 \mathrm{~cm}, \mathrm{QR}=5 \mathrm{~cm}, \angle \mathrm{Q}=120^{\circ}$, $\angle \mathrm{P}=105^{\circ}$ and $\angle \mathrm{R}=135^{\circ}$ ? If not why?

## LEVEL - II

1. Construct a parallelogram PQRS in which $\mathrm{PR}=6 \mathrm{~cm}$ and $\mathrm{QS}=4 \mathrm{~cm}$ and the angle between PR and QS is $50^{\circ}$.
2. Construct a square on a diagonal 6 cm long.
3. Construct a rhombus ABCD , given that $\mathrm{AB}=5 \mathrm{~cm}$ and an anlge is $70^{\circ}$.
4. Construct is rhombus whose diagonals are 5 cm and 4 cm .
5. Construct a parallelogram ABCD whose side $\mathrm{AB}=5.5 \mathrm{~cm}$ and its two diagonals are 1 cm and 8 cm .

## MULTIPLE CHOICE QUESTIONS

1. The minimum number of dimensions needed to construct a rectangle is
(A) 1
(B) 2
(C) 3
(D) 4
2. The minimum number of measurements needed to construct a square is
(A) 1
(B) 2
(C) 3
(D) 4
3. In a quadrilateral PQRS , if $\angle \mathrm{P}=\angle \mathrm{R}=100^{\circ}$ and $\angle \mathrm{S}=75^{\circ}$ then $\angle \mathrm{Q}=$ $\qquad$ .
(A) $50^{\circ}$
(B) $85^{\circ}$
(C) $120^{\circ}$
(D) $306^{\circ}$
4. The sum of the angles in a quadrilateral is equal to $\qquad$
(A) 2 right angles
(B) 3 right angles
(C) 4 right angles
(D) 360 right angles
5. If the lengths of two diagonals of a rhombus are 12 cm and 16 cm , then the length of each side of the rhombus is
(A) 10 cm
(B) 14 cm
(C) cannot be determined
(D) none of these
6. If one of the angle measures more than $180^{\circ}$ in a quadrilateral, then that is known as
(A) a parallelogram
(B) a concave quadrilateral
(C) a convex quadrilateral
(D) a trapezium
7. A quadrilateral which has exactly one pair of parallel sides is called
(A) a parallelogram
(B) a rectangle
(C) a trapezium
(D) a kite
8. Which of the following statements is true?
(A) The diagonals of a rectangle are perpendicular.
(B) The diagonals of a rhombus are equal.
(C) Every square is a rhombus.
(D) None of these.
9. The number of measurements required to construct a quadrilateral is
(A) 5
(B) 4
(C) 3
(D) 2
10. To construct a parallelogram, the minimum number of measurements required is
(A) 2
(B) 3
(C) 4
(D) 1
